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BACHELOR OF COMPUTER APPLICATIONS (BCA) (Revised)

Term-End Examination June, 2021

BCS-012 : BASIC MATHEMATICS

Time: 3 hours

Maximum Marks : 100

Note: Question number 1 compulsory. Attempt any three questions from the remaining questions.

1. (a) If
$$A = \begin{bmatrix} 1 & 2 \\ 2 & -1 \end{bmatrix}$$
; $B = \begin{bmatrix} a & 1 \\ b & -1 \end{bmatrix}$ and
$$(A + B)^2 = A^2 + B^2$$
, find a and b.

- (b) If the first term of an AP is 22, the common difference is -4, and the sum to n terms is 64, find n.
- (c) Find the angle between the lines $\overrightarrow{r_1} = 2\overrightarrow{i} + 3\overrightarrow{j} 4\overrightarrow{k} + t(\overrightarrow{i} 2\overrightarrow{j} + 2\overrightarrow{k})$ $\overrightarrow{r_2} = 3\overrightarrow{i} 5\overrightarrow{k} + s(3\overrightarrow{i} 2\overrightarrow{j} + 6\overrightarrow{k}).$
- (d) If α , β are roots of $x^2 2kx + k^2 1 = 0$, and $\alpha^2 + \beta^2 = 10$, find k.

(e) If
$$y = 1 + ln (x + \sqrt{x^2 + 1})$$
, prove that

$$(x^2 + 1) \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 0.$$

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$$f(x) = \begin{cases} x^2, & x > 0 \\ x + 3, & x \le 0 \end{cases}$$

(g)

(a)

2.

Solve the inequality

$$I = \int \frac{x^2}{(1+x)^3} dx.$$
 Use the principle of mathematical induction to show that

triangle whose vertices are (1, 2); (-2, 3)

(c) Draw the graph of the solution set for the following inequalities:
$$2x + y \ge 8$$
, $x + 2y \ge 8$ and $x + y \le 6$

(d) Use De Moivre's theorem to find
$$(i + \sqrt{3})^3$$
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(a) Find the absolute maximum and minimum of the following function:

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$$f(x) = \frac{x^3}{x + 2}$$
 on $[-1, 1]$

3.

(d)

roots:

4.

(b) Reduce the matrix $A = \begin{bmatrix} 5 & 3 & 8 \\ 0 & 1 & 1 \\ 1 & -1 & 0 \end{bmatrix}$ to

(c) If
$$\overrightarrow{a} = \overrightarrow{i} - 2\overrightarrow{j} + \overrightarrow{k}$$
 and $\overrightarrow{c} = \overrightarrow{i} + 2\overrightarrow{j}$ verify that
$$\overrightarrow{a} \times (\overrightarrow{b} \times \overrightarrow{c}) = (\overrightarrow{a} \cdot \overrightarrow{c}) \overrightarrow{b} - (\overrightarrow{a} \cdot \overrightarrow{b}) \overrightarrow{c}.$$

normal form and hence find its rank.

(0, 3) to (2, -1) using integration.(a) Find the quadratic equation with real coefficients and with the following pair of

Find the length of function y = 3 - 2x from

$$\left(\frac{m-n}{m+n}\right); \left(\frac{m+n}{m-n}\right)$$

- (b) If x = a + b, $y = \omega a + b\omega^2$, $z = \omega^2 + b\omega$ (where ω is a cube root of unity and $\omega \neq 1$), show that $xyz = a^3 + b^3$.
- (c) Solve the following system of linear equations using Cramer's rule :

$$x + y = 0$$
; $y + z = 1$; $z + x = 3$

- 5. (a) A software development company took the designing and development job of a website.

 The designing job fetches the company < 2,000 per hour and development job fetches them < 1,500 per hour. The company can devote at most 20 hours per day for designing and atmost 15 hours for development of website. If total hours available for a day is at most 30, find the maximum revenue the software company can get per day.
 - (b) Evaluate $\int x \sqrt{3-2x} dx$. 5
 - (c) Find the vector and Cartesian equations of the line passing through the points (-2, 0, 3) and (3, 5, -2).